

PH351 PROBLEM SET 1

①

$$\textcircled{1} : \omega_0 = \sqrt{\frac{s}{m}} = \left[\frac{16 \text{ N/m}}{0.01 \text{ kg}} \right]^{1/2} = 40 \text{ sec}^{-1}$$

$$f = \frac{\omega_0}{2\pi} = 6.37 \text{ Hz} \quad T = \frac{1}{f} = 0.157 \text{ s}$$

$$\textcircled{2} \textcircled{a} \text{ INITIAL CONDITIONS } \psi(0) = 0 \quad \dot{\psi}(0) = 0.2 \text{ m/s} \quad \omega_0 = 1 \text{ s}^{-1}$$

$$\text{ASSUMING } \psi(t) = A \cos(\omega_0 t + \phi)$$

$$\psi(0) = A \cos \phi$$

$$\dot{\psi}(t) = -\omega_0 A \sin(\omega_0 t + \phi)$$

$$\dot{\psi}(0) = -\omega_0 A \sin \phi$$

$$\text{SOLVE FOR } A = \sqrt{(\psi(0))^2 + \left(\frac{-\dot{\psi}(0)}{\omega_0}\right)^2} = 0.2 \text{ m}$$

$$\tan \phi = \frac{-\dot{\psi}(0)}{\omega_0 \psi(0)} = \infty \quad \text{so } \phi = \pm \pi/2$$

$$\text{SINCE } \dot{\psi}(0) = 0.2 \text{ m/s} > 0 = -\omega_0 A \sin \phi$$

$$\sin \phi \text{ MUST BE NEGATIVE, } \phi = -\pi/2$$

$$\text{FINALLY } \psi(t) = 0.2 \cos(\omega_0 t - \pi/2)$$

YOU WILL GET A DIFFERENT ϕ IF YOU CHOOSE $\psi(t) = A \sin(\omega_0 t + \phi)$

$$\textcircled{2} \textcircled{b} \quad \omega_0 = 0.3 \text{ s}^{-1}$$

$$\psi(0) = -1.2 \text{ m} \quad \dot{\psi}(0) = 0$$

$$\text{AGAIN ASSUMING } \psi(t) = A \cos(\omega_0 t + \phi)$$

② ⑥ $A = \left[(\psi(0))^2 + \left(-\frac{\dot{\psi}(0)}{\omega_0} \right)^2 \right]^{\frac{1}{2}} = 1.2 \text{ m}$

$\tan \phi = -\frac{\dot{\psi}(0)}{\omega_0 \psi(0)} = 0$ SO $\phi = 0$ OR π

SINCE $\psi(0) = A \cos \phi < 0$ AND $A > 0$

WE MUST CHOOSE $\phi = \pi$

$$\psi(t) = 1.2 \cos(\omega_0 t + \pi)$$

③ THE WORDING OF THIS PROBLEM IS AMBIGUOUS

① IF WE CHOOSE TO READ IT AS $A = 0.01 \text{ m}$

$x(t) = A \sin(\omega t + \delta)$

$E = \frac{1}{2} S A^2$ IS INDEPENDENT OF δ

FROM PROBLEM ① $S = 16 \text{ N/m}$

$E = \frac{1}{2} \left(16 \frac{\text{N}}{\text{m}} \right) (0.01 \text{ m})^2 = \underline{8 \times 10^{-4} \text{ Joules}}$

⑥ OTHERWISE COULD INTERPRET TO MEAN:

~~$x(0)$~~ $x(0) = 0.01 \text{ m}$ $\delta = 0.367$

THEN $x(0) = A \sin \delta \rightarrow A = \frac{x(0)}{\sin \delta} = \frac{0.01 \text{ m}}{\sin(0.367)}$

$\delta = 1.263$

$A = \frac{x(0)}{\sin \delta} = 1.05 \times 10^{-2} \text{ m}$

$E = 8.8 \times 10^{-4} \text{ J}$

$A = 0.028 \text{ m}$

$E = \frac{1}{2} S A^2 = \underline{6.2 \times 10^{-3} \text{ J}}$

PROBLEM 1-5, PAIN.

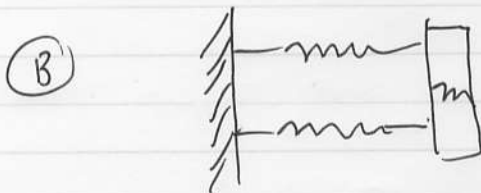
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- IGNORE GRAVITY AND FRICTION
- ASSUMING REST LENGTH OF SPRING = 0



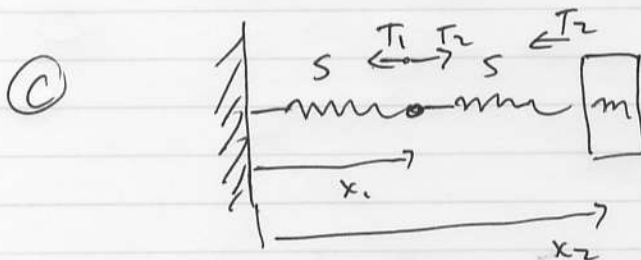
$$F = -Sx$$

$$m\ddot{x} = -Sx \rightarrow \omega_A^2 = \frac{S}{m}$$



OBVIOUSLY $F = -2Sx$

$$m\ddot{x} = -2Sx \quad \omega_B^2 = \frac{2S}{m}$$



$$T_1 = \text{TENSION IN SPRING 1} \\ = -Sx_1$$

$$T_2 = \text{TENSION IN SPRING 2} \\ = -S(x_2 - x_1)$$

$$\text{FORCE ON MASS} = T_2 \quad \text{SO}$$

$$m\ddot{x}_2 = -S(x_2 - x_1)$$

NEED TO SOLVE FOR x_1

USE: $T_1 = T_2$ OTHERWISE SPRING AT x_1 WOULD ACCELERATE,

$$\text{SO: } -Sx_1 = -S(x_2 - x_1) \Rightarrow x_1 = \frac{x_2}{2}$$

$$\text{THEN: } m\ddot{x}_2 = -S\left(x_2 - \frac{x_2}{2}\right) = -\frac{S}{2}x_2$$

$$\omega_C^2 = \frac{S}{2m}$$

$$\boxed{\omega_B^2 : \omega_A^2 : \omega_C^2 = 1 : 2 : 4}$$